

Problem 4.3

$$x(t) = 18t \text{ and } y(t) = 4t - 4.9t^2$$

a.) position vector:

$$\vec{r}(t) = (18t)\hat{i} + (4t - 4.9t^2)\hat{j}$$

b.) velocity function:

$$\begin{aligned}\vec{v}(t) &= \frac{d\vec{r}}{dt} \\ &= \frac{d[(18t)\hat{i} + (4t - 4.9t^2)\hat{j}]}{dt} \\ &= [18\hat{i} + (4 - 9.8t)\hat{j}](\text{m/s})\end{aligned}$$

$$x(t) = 18t \text{ and } y(t) = 4t - 4.9t^2$$

c.) acceleration function:

$$\begin{aligned}\bar{a}(t) &= \frac{d\bar{v}}{dt} \\ &= \frac{d[18\hat{i} + (4 - 9.8t)\hat{j}]}{dt} \\ &= (-9.8 \text{ m/s}^2) \hat{j}\end{aligned}$$

d.) at $t = 3$ seconds:

$$\begin{aligned}\bar{r}(t) &= (18t)\hat{i} + (4t - 4.9t^2)\hat{j} \\ &= (18(3))\hat{i} + (4(3) - 4.9(3)^2)\hat{j} \\ &= [54\hat{i} - 32.1\hat{j}] \text{ meters}\end{aligned}$$

$$\bar{a}(t) = (-9.8 \text{ m/s}^2) \hat{j}$$

$$\begin{aligned}\bar{v}(t) &= [18\hat{i} + (4 - 9.8t)\hat{j}] \\ &= [18\hat{i} + (4 - 9.8(3))\hat{j}] \\ &= [18\hat{i} - 25.4\hat{j}] \text{ (m/s)}\end{aligned}$$